## Assignment \#6-key

1. (a) $(\mathrm{Fh} \wedge \mathrm{Gh})$
(b) $\forall x(F x \supset G x)$
(c) $(F h \supset \exists x(F x \wedge \neg G x))$
2. 

(a) Not everyone who ate rice got sick.

Not All S are P.
Subject: People who ate rice. $\quad(\mathrm{Px} \wedge \mathrm{Rx})$
Predicate: Things that got sick $S x$
$\neg \forall x((P x \wedge R x) \supset S x) \quad$ or $\quad \exists x((P x \wedge R x) \wedge \neg S x)$
(b) Some beautiful people are not good and will not get to heaven.

Some $S$ are not $P$.
Subject: Beautiful people. $\quad(P x \wedge B x)$
Predicate: Things that are either good or will get to heaven. $\quad(G x \vee W x)$
$\exists x((P x \wedge B x) \wedge \neg(G x \vee W x)) \quad$ or $\quad \neg \forall x((P x \wedge B x) \supset(G x \vee W x))$
(c) No one will be appreciated unless they are either beautiful or rich.

In other words: If you are a person and you are not beautiful or rich, then you will not be appreciated.
Subject: People who are not either beautiful or rich. $\quad(P x \wedge \neg(B x \vee D x))$
Predicate: Things that are not appreciated. $\neg \mathrm{Ax}$
$\forall x((P x \wedge \neg(B x \vee D x)) \supset \neg A x) \quad$ (No $S$ are $P$.)
equivalent to
$\neg \exists \mathrm{x}((\mathrm{Px} \wedge \neg(\mathrm{Bx} \vee \mathrm{Dx})) \wedge \mathrm{Ax}) \quad($ Not some S are not P$)$
OR
Subject: People. Px
Predicate: Things that, if not beautiful or rich, are not appreciated. $(\neg(B x \vee D x) \supset \neg A x)$
$\forall x(P x \supset(\neg(B x \vee D x) \supset \neg A x)) \quad($ All S are P.)
equivalent to
$\neg \exists \mathrm{x}(\mathrm{Px} \wedge \neg(\neg(\mathrm{Bx} \vee \mathrm{Dx}) \supset \neg \mathrm{Ax})) \quad($ Not some S are not P$)$
3. Translate the following from $\mathbf{Q L}$ into English using the translation key from \#2.
(a) $\neg \forall x((P x \wedge(B x \wedge G x)) \supset(D x \vee A x))$

Not everyone who is beautiful and good is either rich or appreciated.
There are people who are beautiful and good and neither rich nor appreciated.
(b) $\quad \forall x((P x \wedge((D x \wedge F x) \vee A x)) \supset(G x \vee B x))$

Everyone who is either rich and famous or appreciated is either good or beautiful.
There is no one who is either rich and famous or appreciated and who isn't either good or beautiful.
4. (a) Some professors listen to some of their students.
(b) Some professors don't read the poetry they haven't written.
(c) $\exists x(S x \wedge \exists y((B y \wedge R x y) \wedge \exists z((F z \wedge H x z) \wedge A z y x)))$
(d) $\quad \exists \mathrm{x}((\mathrm{Sx} \wedge \mathrm{Dx}) \wedge \neg \mathrm{Gx}) \wedge(\exists \mathrm{y}(\mathrm{Py} \wedge \mathrm{Rxy}) \wedge \exists \mathrm{z}(\mathrm{Pz} \wedge \mathrm{W} x z)))$

