



ER = EPR? Topology and Quantum Entanglement

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Abstract

Maldacena & Susskind's "ER=EPR" hypothesis claims that two physical systems in a quantum entangled ("EPR", or Einstein-Podolsky-Rosen) state are connected by an Einstein-Rosen ("ER") wormhole. More generally, it claims that spacetime topology is the "dual" of quantum entanglement: physical systems in a quantum entangled state can be described as systems connected by a wormhole, and *vice-versa*. Our project's goals are to assess the motivations for "ER=EPR", including AdS/CFT theory and the Black Hole Firewall Problem, and to construct a conceptual map that relates characteristics of wormholes to characteristics of entanglement.

Motivations for ER=EPR [1]

1. Correspondence between extended AdS-Schwarzschild spacetime and entangled vacuum state of a CFT.
2. Resolves Firewall Problem.
3. No superluminal signals, and no creation and/or increase by LOCC.

Firewall Paradox

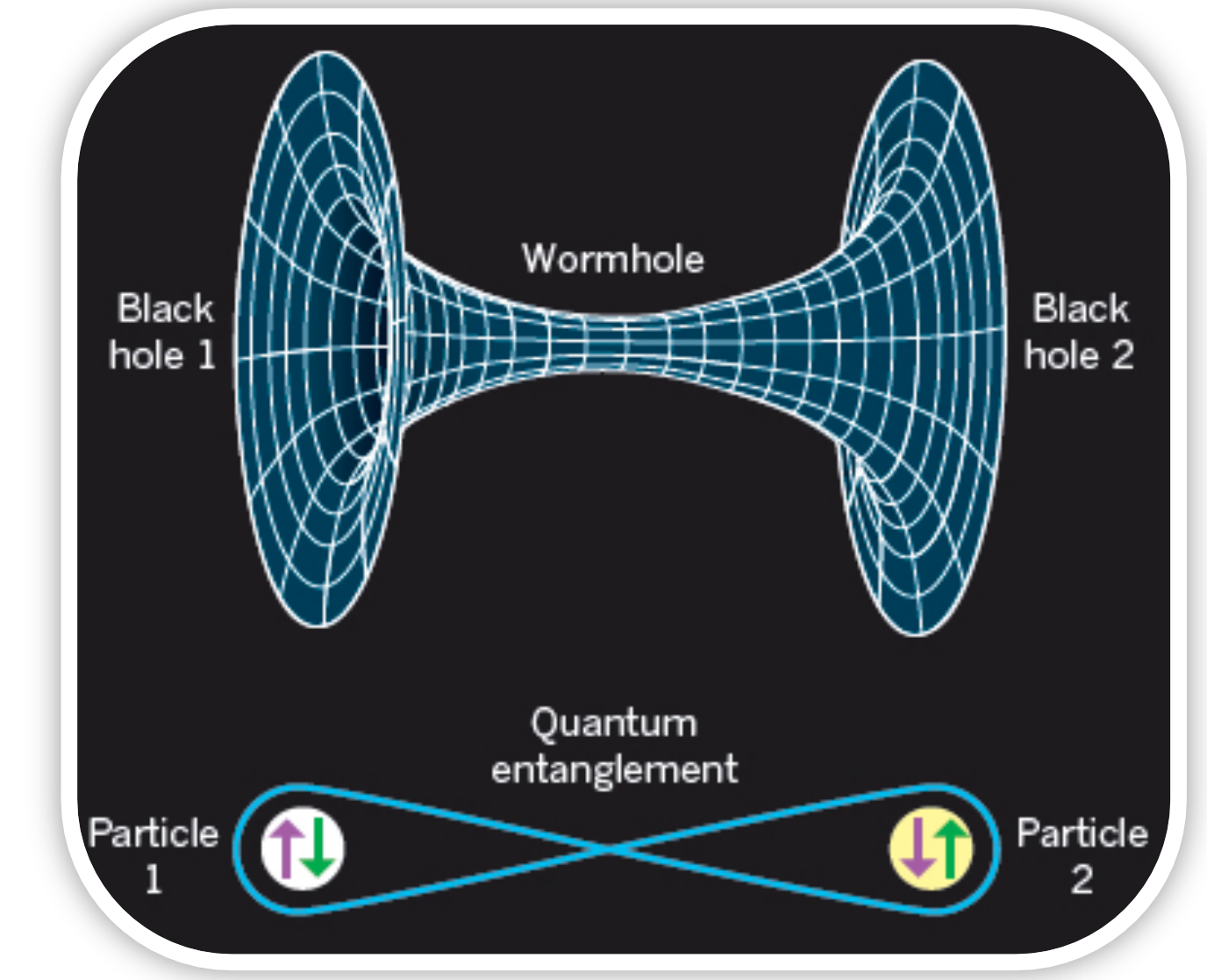
- (i) B is maximally entangled with A .
- (ii) B is maximally entangled with R_B .
- (iii) B cannot be maximally entangled with two systems.

ER=EPR Resolution

Deny (i): When R_B is distilled, it "disrupts" A via a wormhole connection.

Conceptual Map

Quantum Entanglement	Wormhole
Entanglement Entropy $S_A = -\text{Tr}(\rho_A \log \rho_A)$ Used to describe the extent to which a bipartite system AB is entangled.	Maximin Cross-Sectional Area of Throat *Under ER=EPR, a wormhole's maximin cross-sectional area is considered the dual of entanglement entropy.
No Superluminal Signaling Quantum entanglement cannot be used to send superluminal signals.	Non-traversability Any future-directed curve that passes through a wormhole must become space-like along some of its extent.
Quantum Cloning [2] If a multipartite entangled state is the result of cloning one of the substates B of a bipartite entangled state AB, and: <ul style="list-style-type: none"> (1) all B-clones remain entangled with A; (2) entanglements of different subsystems do not influence each other; then it facilitates superluminal signaling.	Topology Change If a wormhole has formed as a result of topology change, and if it violates the null energy condition, then it is traversable, which indicates superluminal signaling.
Entanglement Non-detectability There is no observable that represents entanglement in terms of a linear operator.	Wormhole Non-detectability There is no local curvature measurement that can distinguish between a one-sided black hole spacetime and a two-sided black hole (i.e., wormhole) spacetime.
Entanglement Conservation For a bipartite system AB, the entanglement entropy S_A of subsystem A is invariant under local operations.	Area Conservation The maximin cross-sectional area of a wormhole is invariant under local operations performed near its mouths.
Entanglement Monogamy [3] If A and B are maximally entangled, then neither A nor B is entangled with any other system C.	Wormhole Monogamy If a "maximal" wormhole connects regions A and B, then neither A nor B can be connected by a wormhole to any other region C.



Future Work

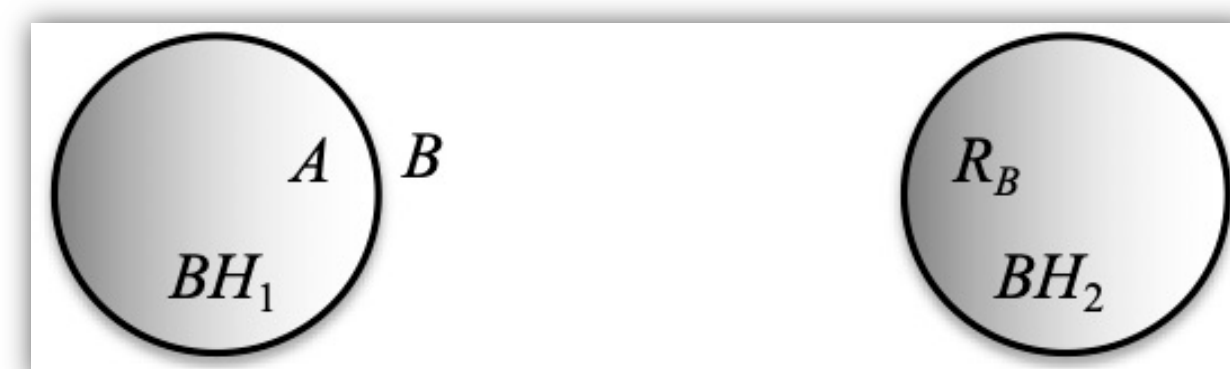
We have now created a conceptual map between entanglement and wormholes. While this map exposes intriguing relations that support ER=EPR, additional questions remain. First, we need to further specify the meaning of non-detectability, since it risks making ER=EPR unverifiable. Second, entanglement monogamy is potentially contradictory to ER=EPR's resolution to the Firewall Paradox: RB cannot be wormhole-connected with A since it is maximally entangled with B. Finally, more conceptual work could be done on the relation between ER=EPR and recent derivations of the Einstein equations from entanglement first principles.

Select Works Cited

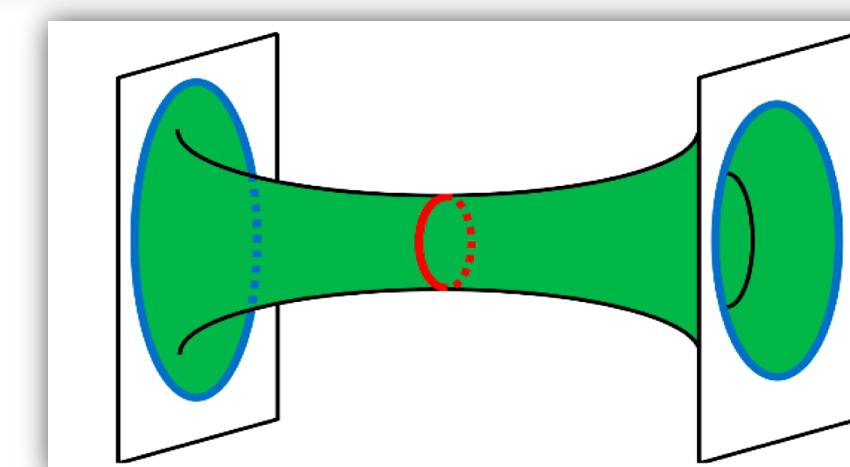
- [1] Maldacena, J. & L. Susskind (2013) "Cool Horizons for Entangled Black Holes", *Fortschritte der Physik* 61, 781.
- [2] Remmen, G., N. Bao, & J. Pollack (2015) "Splitting spacetime and cloning qubits: linking no-go theorems across the ER=EPR duality", *Fortschritte der Physik* 63, 705.
- [3] Gharibyan, H. & R. Penna (2014) "Are entangled particles connected by wormholes? Evidence for the ER = EPR conjecture from entropy inequalities", *Physical Review D* 89, 066001-1.

Acknowledgement

The authors thank NYU Tandon School of Engineering's Office of Undergraduate Academics for generous funding of the project.



P1. An Illustration of Firewall Paradox



P2. Maximin Cross Sectional Area of Throat